

## 6-1

# Graphing Systems of Equations

### What You'll Learn

Scan the text under the *Now* heading. List two things you will learn about in the lesson.

1. Name and classify  
Systems
2. Solve systems by  
graphing

Work on this for the next couple of minutes. I will call on one of you afterward.

## Active Vocabulary

**Review Vocabulary** Make a table of values which satisfy the equation  $x + y = 13$ . (Lesson 3-1)

$y = -x + 13$

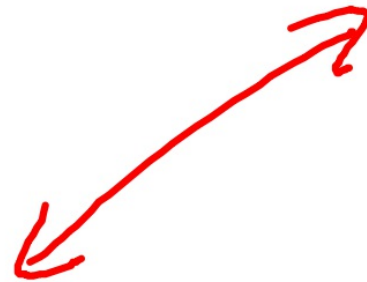
$x$	0	1	3	10	...	---			
$y$	13	12	10	3					

Is it possible to make a table that shows all ordered pairs that satisfy this equation? Justify your answer.

No... Infinite

How can you show all of the ordered pairs for the equation?

with a picture!



**New Vocabulary** Match the term with its definition by drawing a line.

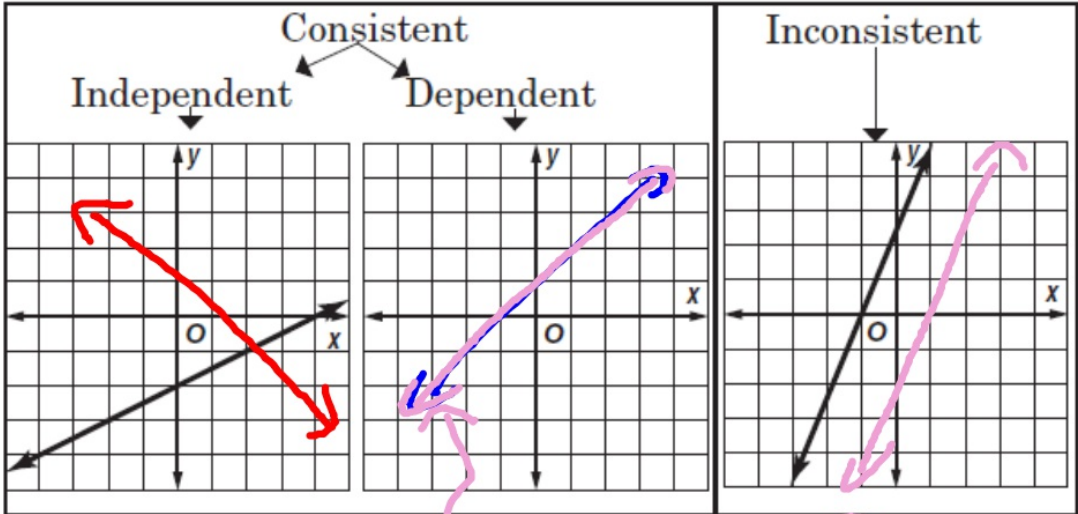
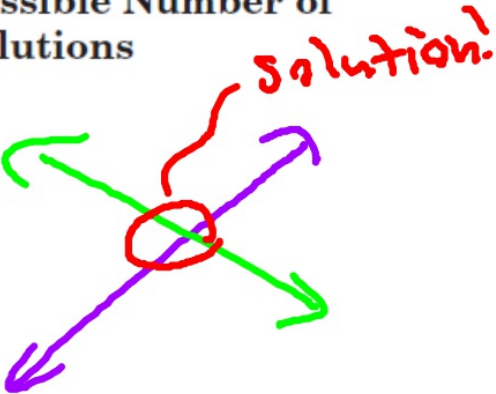
- consistent* a set of two or more equations that contain the same variables
- inconsistent* a system of equations that has at least one solution
- system of equations* a system of equations that has an infinite number of solutions
- independent* a system of equations that has exactly one solution
- dependent* a system of equations that has no solutions
-

# Main Idea

# Details

Possible Number of Solutions

Add a line to each graph so that the given condition is satisfied.

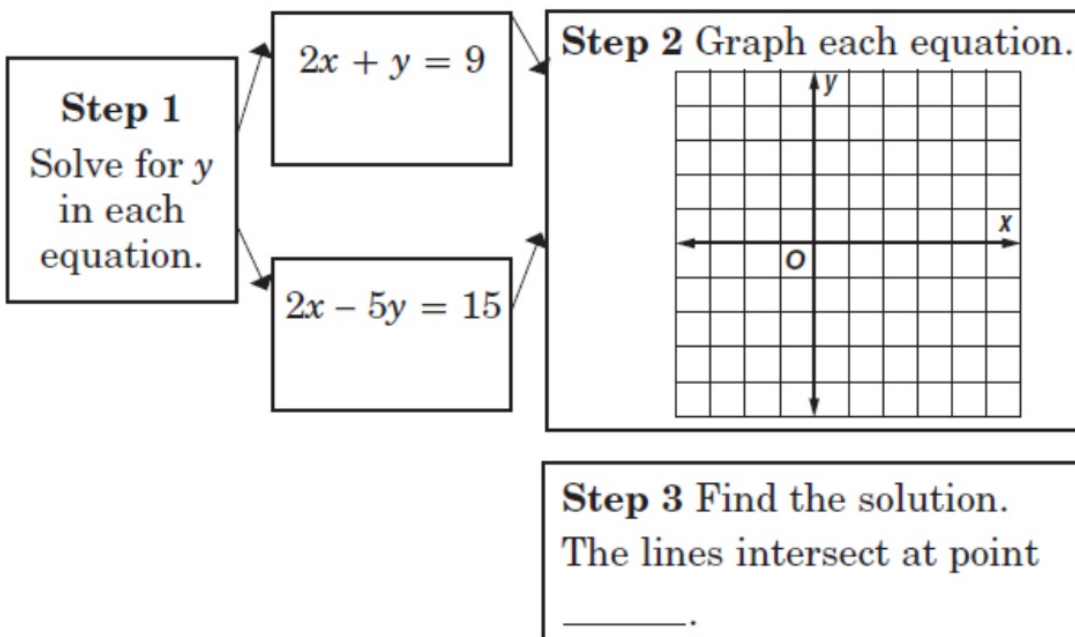


two lines overlap.

parallel lines never intersect!

## Solve by Graphing

Solve the system of equations by graphing.

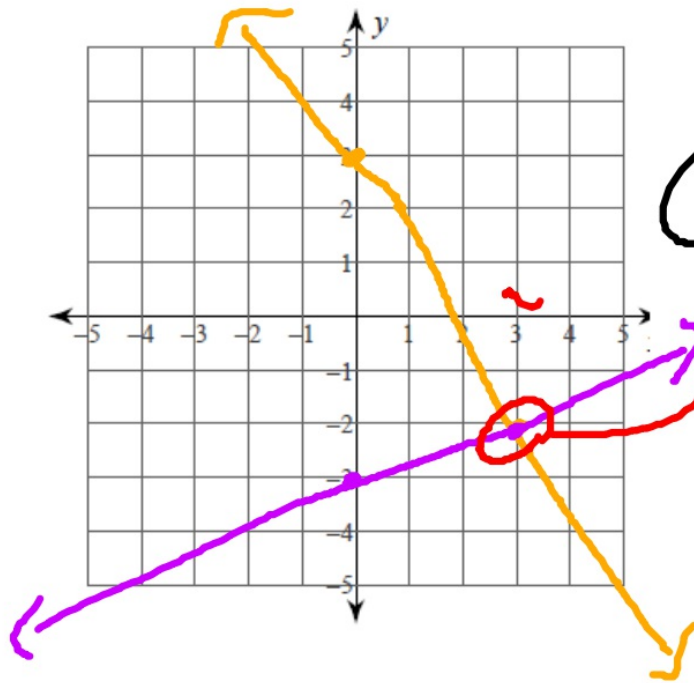


Solve each system by graphing.

$$y = mx + b$$

$$1) \ y = -\frac{5}{3}x + 3$$

$$y = \frac{1}{3}x - 3$$



① Graph each equation.

② Find the point of intersection.

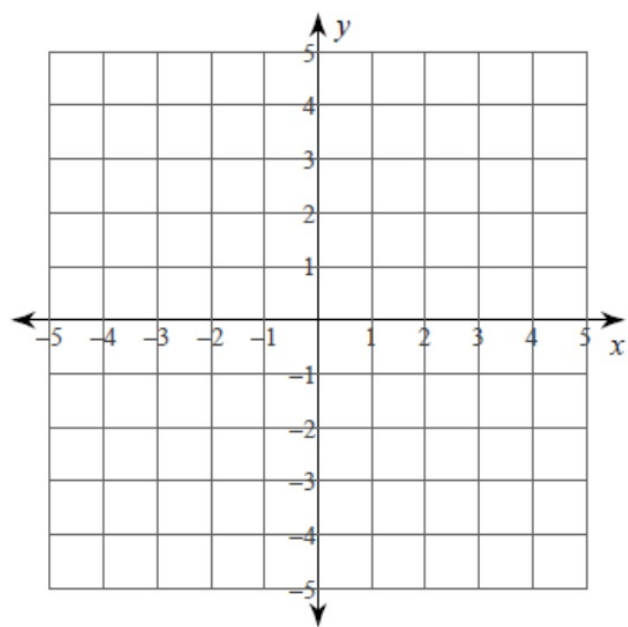
③ check it!

$$(3, -2)$$
$$-2 = -\frac{5}{3}(3) + 3$$
$$-2 = -5 + 3 \checkmark$$
$$-2 = \frac{1}{3}(3) - 3$$
$$-2 = 1 - 3 \checkmark$$

**Solve each system by graphing.**

2)  $y = 4x + 3$

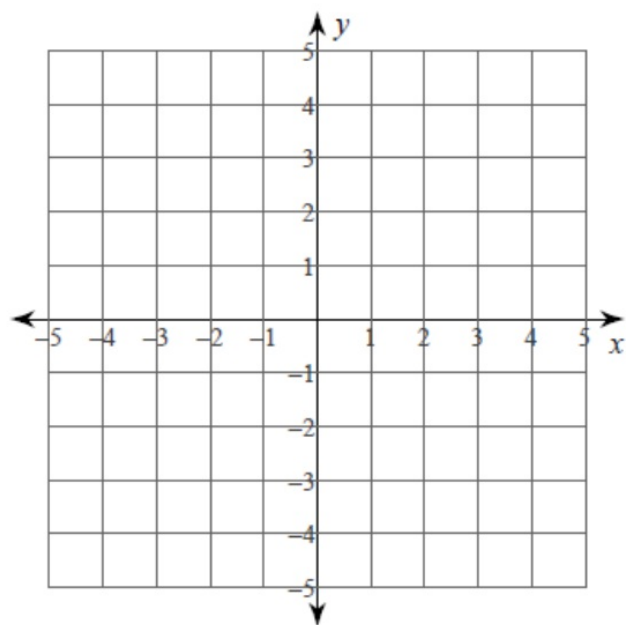
$y = -x - 2$



**Solve each system by graphing.**

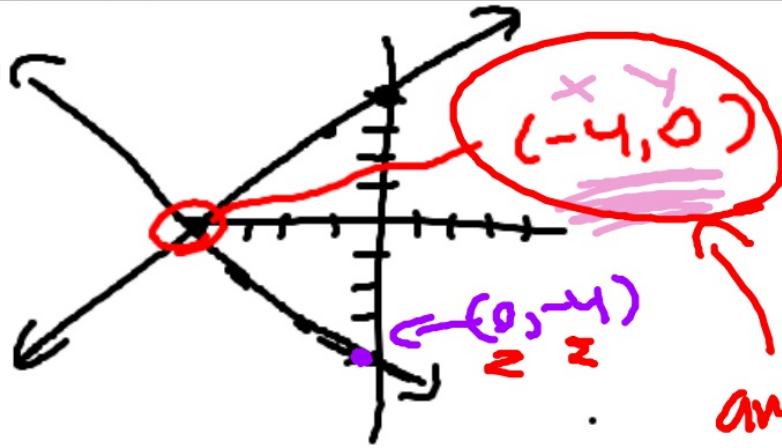
4)  $y = -1$

$$y = -\frac{5}{2}x + 4$$





7



$$(0) = (-4) + 4 \quad \checkmark$$

$$0 = -(-4) - 4 \quad \checkmark$$

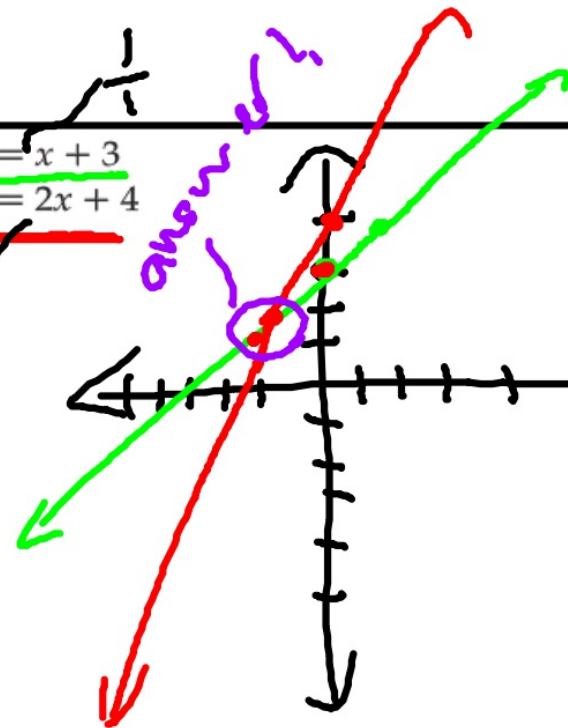
answer!

7.  $y = x + 4$   
 $y = -x - 4$

$-4 = 0 + 4$   
 $0 = 0 - 4$   
 $-4 = 0 - 4$

8.  $y = x + 3$   
 $y = 2x + 4$

2/1



1 Graph!

2 Graph!

3 Find it!

**Example 1**

Use the graph at the right to determine whether each system is *consistent* or *inconsistent* and if it is *independent* or *dependent*.

1.  $y = -3x + 1$

$y = 3x + 1$  **consistent and independent**

2.  $y = 3x + 1$

$y = x - 3$  **consistent and independent**

3.  $y = x - 3$

$y = x + 3$  **inconsistent**

4.  $y = x + 3$

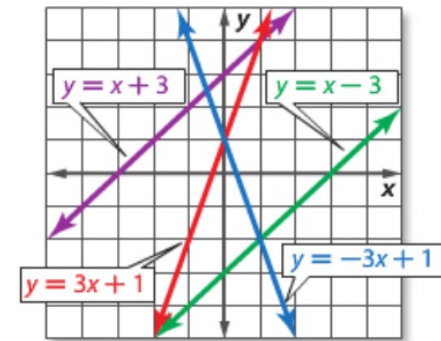
$x - y = -3$  **consistent and dependent**

5.  $x - y = -3$

$y = -3x + 1$  **consistent and independent**

6.  $y = -3x + 1$

$y = x - 3$  **consistent and independent**

**Example 2**

Graph each system and determine the number of solutions that it has. If it has one solution, name it. **7–8. See margin.**

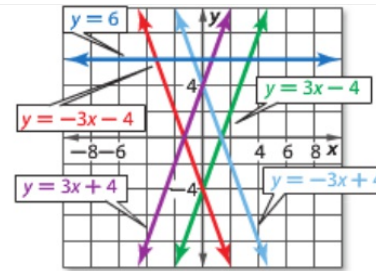
7.  $y = x + 4$

8.  $y = x + 3$



**Example 1**

Use the graph at the right to determine whether each system is *consistent* or *inconsistent* and if it is *independent* or *dependent*.



- |                                    |                                   |
|------------------------------------|-----------------------------------|
| 10. $y = 6$<br>$y = 3x + 4$        | 11. $y = 3x + 4$<br>$y = -3x + 4$ |
| 12. $y = -3x + 4$<br>$y = -3x - 4$ | 13. $y = -3x - 4$<br>$y = 3x - 4$ |
| 14. $3x - y = -4$<br>$y = 3x + 4$  | 15. $3x - y = 4$<br>$3x + y = 4$  |

$y = mx + b$

**Example 2**

Graph each system and determine the number of solutions that it has. If it has one solution, name it. **16–24. See margin.**

- |                                    |                                   |                                     |
|------------------------------------|-----------------------------------|-------------------------------------|
| 16. $y = -3$<br>$y = x - 3$        | 17. $y = 4x + 2$<br>$y = -2x - 3$ | 18. $y = x - 6$<br>$y = x + 2$      |
| 19. $x + y = 4$<br>$3x + 3y = 12$  | 20. $x - y = -2$<br>$-x + y = 2$  | 21. $x + 2y = 3$<br>$x = 5$         |
| 22. $2x + 3y = 12$<br>$2x - y = 4$ | 23. $2x + y = -4$                 | 24. $2x + 2y = 6$<br>$5y + 5x = 15$ |

- 10. consistent and independent
- 11. consistent and independent
- 12. inconsistent
- 13. consistent and independent
- 14. consistent and dependent
- 15. consistent and independent

20.  $x - y = -2$       $x - y = -2$

$$\begin{array}{r} x - y = -2 \\ -x + y = 2 \\ \hline -y = -x - 2 \\ \hline y = x + 2 \end{array}$$

$y = x + 2$

$$\begin{array}{r} -x + y = 2 \\ +x \\ \hline y = x + 2 \end{array}$$

$y = x + 2$

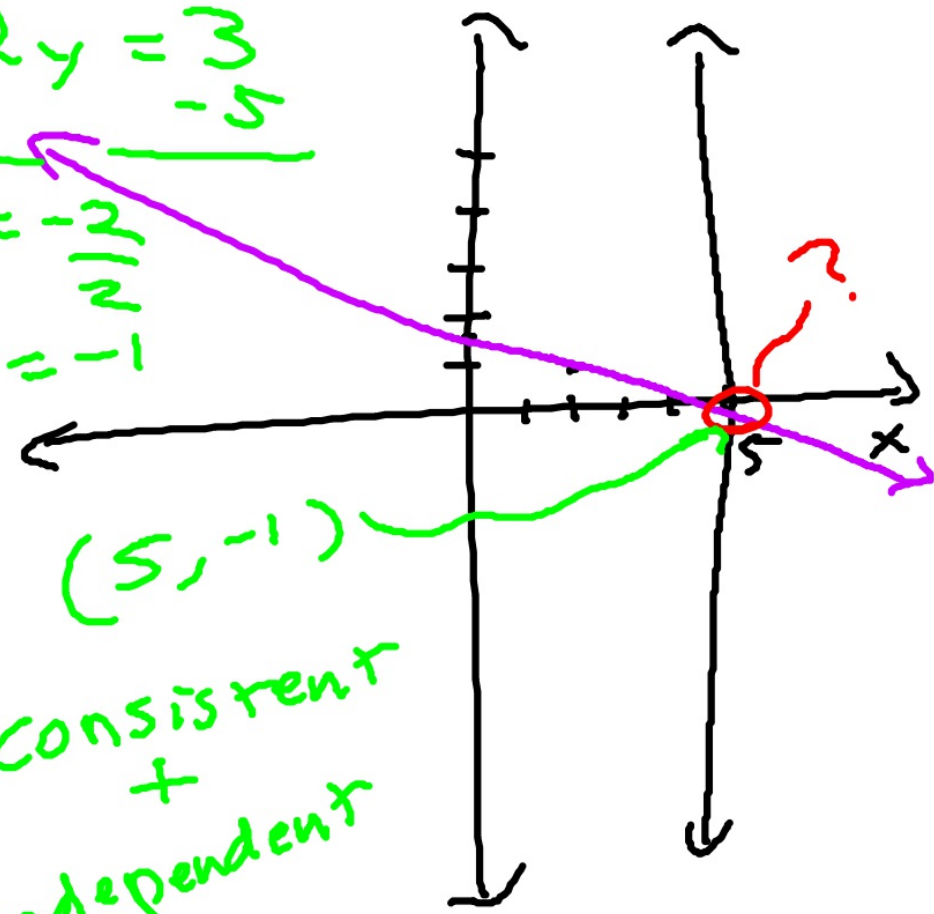
consistent + dependent.

21.  $x + 2y = 3$

$x = 5$

SO...  
 $x + 2y = 3$   
 $-5 + 2y = 3$   
 $2y = 8$   
 $y = 4$

$x + 2y = 3$   
 $-x$   
 $2y = -x + 3$   
 $y = -\frac{1}{2}x + \frac{3}{2}$



consistent + independent