

LESSON 8-4 Special Products

5-Minute Check

Over Lesson 8-3

- 4** Which expression represents the area of the figure? area = length x width

$2a - 3$



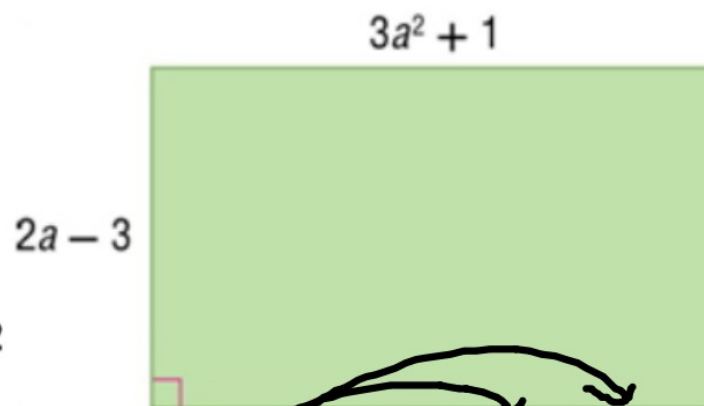
- A. $6a^3 - 9a^2 + 2a - 3$ units²
- B. $5a^3 - 2a^2 + 2a - 2$ units²
- C. $4a^3 - 2a^2 + a - 2$ units²
- D. $3a^3 - a^2 + 3a + 3$ units²

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Over Lesson 8-3

4 Which expression represents the area of the figure?



→ A. $6a^3 - 9a^2 + 2a - 3 \text{ units}^2$

B. $5a^3 - 2a^2 + 2a - 2 \text{ units}^2$

C. $4a^3 - 2a^2 + a - 2 \text{ units}^2$

D. $3a^3 - a^2 + 3a + 3 \text{ units}^2$

Handwritten work showing the multiplication of the rectangle's dimensions:

$$(3a^2 + 1)(2a - 3)$$

$$6a^3 - 9a^2 + 2a - 3$$

8-4 Special Products

"difference of squares"

Yesterday, there were a couple of problems that resulted in a "special" case;

last night's
HW →

$$19. (7n - 6)(7n - 6)$$

$$19. 49n^2 - 84n + 36$$

$$20. (12t - 5)(12t + 5) \quad 144t^2 - 25$$

perfect squares!

$12t$	-5
$12t$	$144t^2 - 60t$
5	$60t - 25$

cancelled!

KeyConcept Square of a Difference

Words The square of $a - b$ is the square of a minus twice the product of a and b plus the square of b .

Symbols $(a - b)^2 = (a - b)(a - b)$ Example $(x - 3)^2 = (x - 3)(x - 3)$
 $= a^2 - 2ab + b^2$ $= x^2 - 6x + 9$

this also exist for sum...

KeyConcept Product of a Sum and a Difference

Words The product of $a + b$ and $a - b$ is the square of a minus the square of b .

Symbols $(a + b)(a - b) = (a - b)(a + b)$
 $= a^2 - b^2$

KeyConcept Square of a Sum





KeyConcept Product of a Sum and a Difference

Words The product of $a + b$ and $a - b$ is the square of a minus the square of b .

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KeyConcept Square of a Difference

Words The square of $a - b$ is the square of a minus twice the product of a and b plus the square of b .

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$$(a - b)^2 = (a - b)(a - b)$$
$$= a^2 - 2ab + b^2$$
 Example
$$(x - 3)^2 = (x - 3)(x - 3)$$
$$= x^2 - 6x + 9$$

In this chapter, it was meant to help remember special patterns when it comes to multiplying polynomials together.

Example 4 Product of a Sum and a Difference

Find $(2x^2 + 3)(2x^2 - 3)$.

$$(a + b)(a - b) = a^2 - b^2$$

Product of a sum and a difference

$$(2x^2 + 3)(2x^2 - 3) = (2x^2)^2 - (3)^2$$

$a = 2x^2$ and $b = 3$

$$= 4x^4 - 9$$

Simplify.

These will be important patterns to recognize when it comes to *doing this in reverse* (we will be doing this later).

“Factoring”

Besides that, we can multiply by using the box method from yesterday!~

Check Your Understanding

 = Step-by-Step Solutions begin on page R13.



Examples 1–2 Find each product. 4. $9m^2 - 24m + 16$ 5. $g^2 - 8gh + 16h^2$ 6. $9c^2 + 36cd + 36d^2$

1. $(x + 5)^2$ $x^2 + 10x + 25$ 2. $(11 - a)^2$ $121 - 22a + a^2$ 3. $(2x + 7y)^2$ $4x^2 + 28xy + 49y^2$
4. $(3m - 4)(3m - 4)$ 5. $(g - 4h)(g - 4h)$ 6. $(3c + 6d)^2$ D y

① $(x + 5)(x + 5)$

	x	5
x	x^2	$5x$
5	$5x$	25

check

$$x^2 + 10x + 25$$

Check Your Understanding

 = Step-by-Step Solutions begin on page R13.



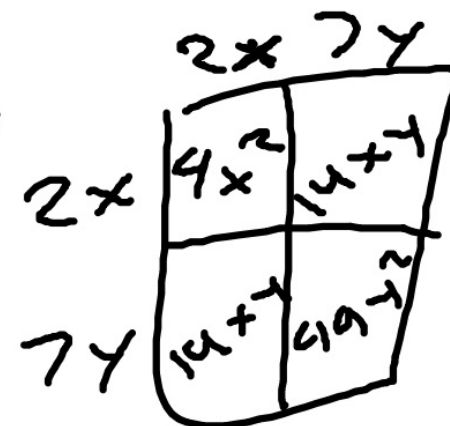
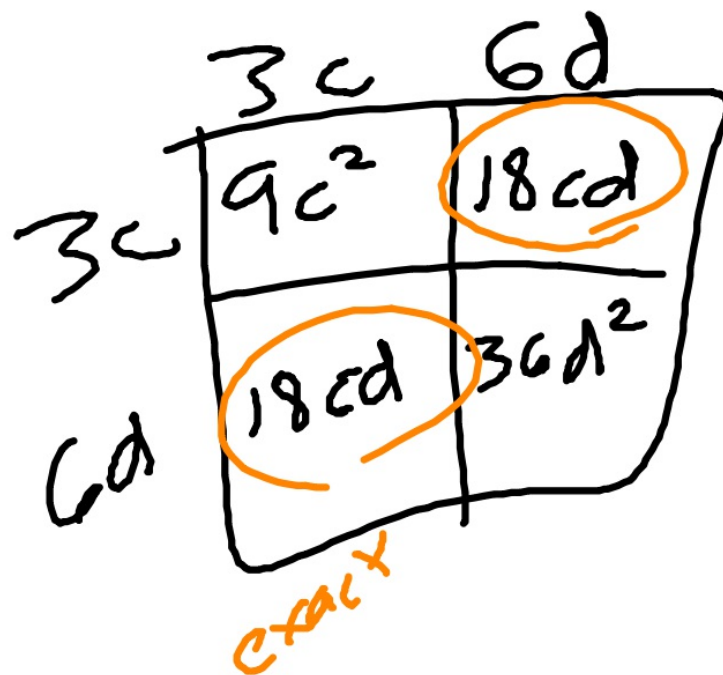
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 D y

$$(3c + 6d)(3c + 6d)$$

④ $9m^2 + 16$
 ~~$-24m$~~



Example 3

7. **GENETICS** The color of a Labrador retriever's fur is genetic. Dark genes D are dominant over yellow genes y . A dog with genes DD or Dy will have dark fur. A dog with genes yy will have yellow fur. Pepper's genes for fur color are Dy , and Ramiro's are yy .

	D	y
D	DD	Dy
y	Dy	yy

- a. Write an expression for the possible fur colors of Pepper's and Ramiro's puppies.
- b. What is the probability that a puppy will have yellow fur?

hint:

$$\begin{array}{c}
 \begin{array}{|c|c|}
 \hline
 \overbrace{a+b} \\
 \hline
 \begin{array}{|c|c|}
 \hline
 a & b \\
 \hline
 \begin{array}{|c|c|}
 \hline
 a & b \\
 \hline
 \begin{array}{|c|c|}
 \hline
 a^2 & ab \\
 \hline
 ab & b^2 \\
 \hline
 \end{array}
 \end{array}
 \end{array}
 \end{array}
 \end{array}
 = a^2 + ab + ab + b^2
 \end{array}$$

$(a+b)^2 = a^2 + ab + ab + b^2$

25%

a. $DD + 2Dy + yy$

$$\textcircled{8} \quad (\underline{a-3})(\underline{a+3})$$

$$\underline{a^2} - \underline{9}$$

$$\textcircled{9} \quad (x+5)(x-5) \\ = x^2 - 25$$

	a	-3
a	a^2	$-3a$
3	$3a$	-9

cancel!!

Examples 1-2 Find each product.

12. $(a + 10)(a + 10)$ $a^2 + 20a + 100$

14. $(h + 7)^2$ $h^2 + 14h + 49$

16. $(8 - m)^2$ $64 - 16m + m^2$

18. $(2b + 3)^2$ $4b^2 + 12b + 9$

20. $(8h - 4n)^2$ $64h^2 - 64hn + 16n^2$

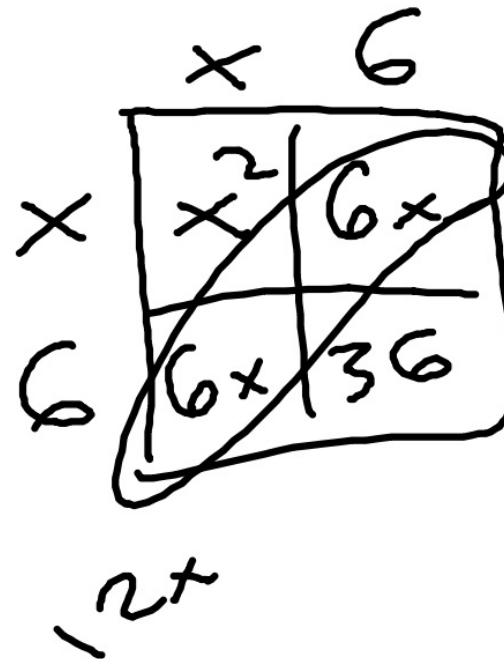
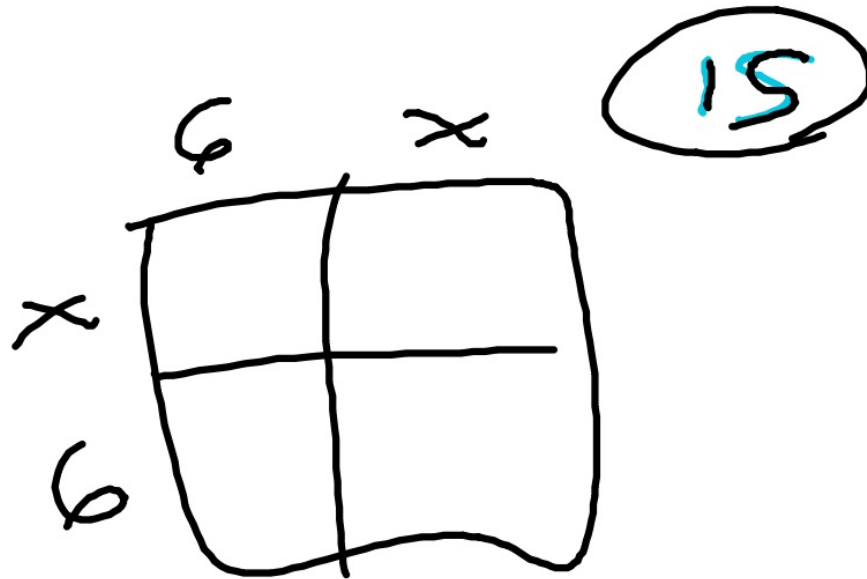
13. $(b - 6)(b - 6)$ $b^2 - 12b + 36$

15. $(x + 6)^2$ $x^2 + 12x + 36$

17. $(9 - 2y)^2$ $81 - 36y + 4y^2$

19. $(5t - 2)^2$ $25t^2 - 20t + 4$

$(x+6)(x+6)$



Examples 1-2 Find each product.

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(17)

$(9 - 2y)(9 - 2y)$

	9	-2y
9	81	<u>-18y</u>
-2y	<u>-18y</u>	$4y^2$

Example 3

21. **GENETICS** The ability to roll your tongue is inherited genetically from parents if either parent has the dominant trait T . Children of two parents without the trait will not be able to roll their tongues.

	T	t
T	TT	Tt
t	Tt	tt

- a. Show how the combinations can be modeled by the square of a sum. $(T + t)^2 = T^2 + 2Tt + t^2$
- b. Predict the percent of children that will have both dominant genes, one dominant gene, and both recessive genes. $TT: 25\%; Tt: 50\%; tt: 25\%$

Example 4

Find each product. 22-44. See margin.

conjugate!

22. $(u + 3)(u - 3)$

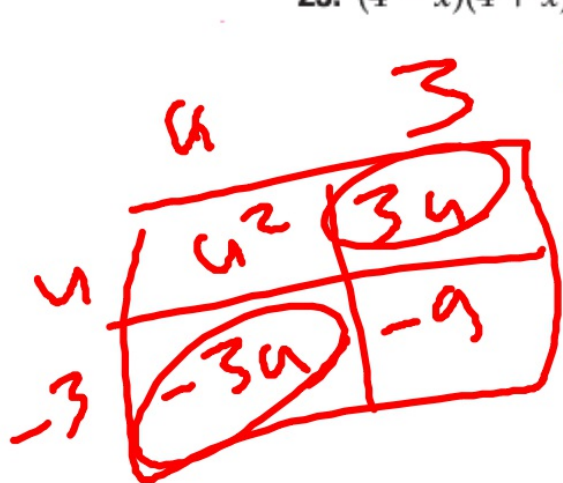
23. $(b + 7)(b - 7)$

24. $(2 + x)(2 - x)$

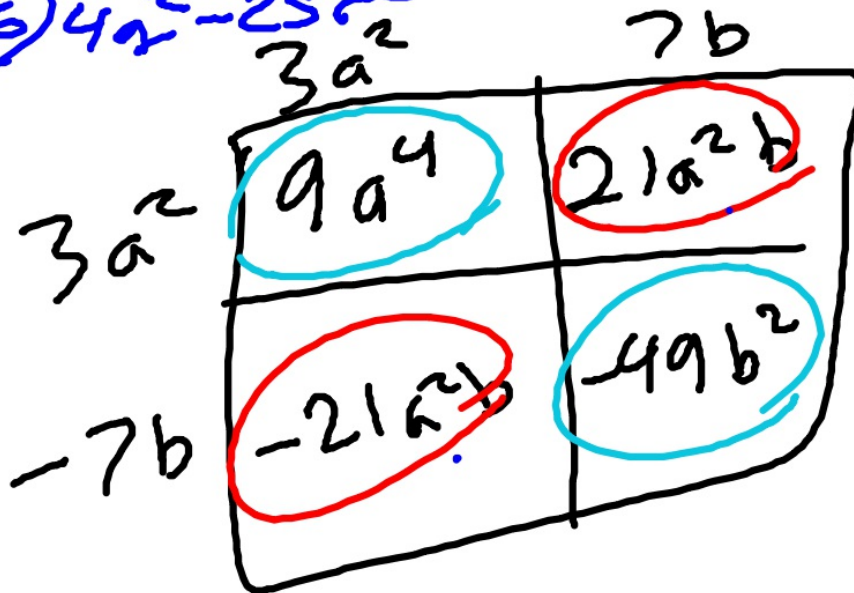
25. $(4 - x)(4 + x)$

26. $(2q + 5r)(2q - 5r)$

27. $(3a^2 + 7b)(3a^2 - 7b)$



$(26) 4a^2 - 25r^2$



cancel!!!