

Lesson

Negative Exponents

Real-World Link

ects The table shows the approximate wing beats per minute for certain insects.

Insect	Wing Beats per Minute
house fly	10,000
small butterfly	100

Write a ratio in simplest form that compares the number of wing beats

for a butterfly to a housefly.

$$\frac{1}{100}$$

Write the ratio as a fraction with an exponent in the denominator and as a decimal.

$$\frac{1}{10^2}; 0.01$$

Handwritten:
 $\frac{100}{10000}$
 $\frac{1}{10^2}$



Essential Question

WHY is it helpful to write numbers in different ways?



Common Core State Standards

Content Standards
8.EE.1

MP Mathematical Practices
1, 3, 4, 7

Complete the 1st 4 rows



Standard Form

3. Complete the 1st 4 rows of the table showing the exponential and standard forms of power of 10.

4. What operation is performed when you move down the table?

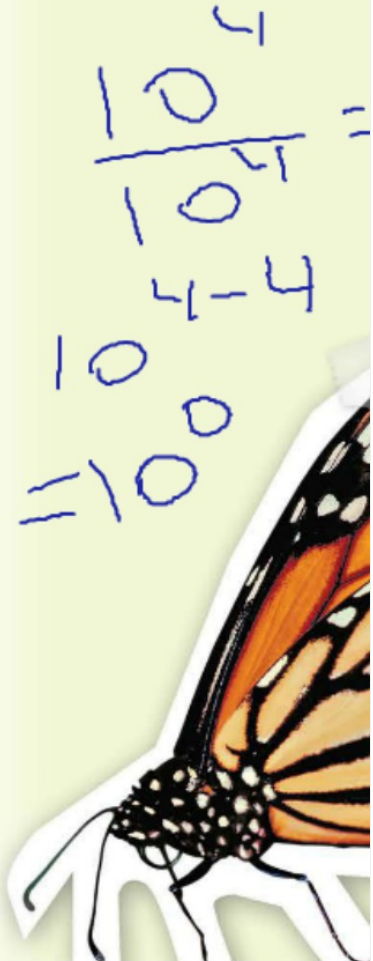
division

5. What happens to the exponent?

It decreases by one.

6. Extend the table to include the next three entries.

Exponential Form	Standard Form
10^3	1,000
10^2	100
10^1	10
10^0	1
10^{-1}	$\frac{1}{10}$ or 0.1
10^{-2}	$\frac{1}{100}$ or 0.01
10^{-3}	$\frac{1}{1,000}$ or 0.001



Negative powers are the result of repeated division.

Examples

Write each expression using a positive exponent.

1. 6^{-3}

2. a^{-5}

$\frac{6^{-3}}{1} = \frac{1}{6^3}$ Definition of negative exponent

$\frac{a^{-5}}{1} = \frac{1}{a^5}$ Definition of negative exponent

Got it? Do these problems to find out.

a. 7^{-2}

b. b^{-4}

c. 5^0

d. m^{-3}

Examples

Write each fraction as a negative exponent

10.

$\frac{1}{7^2}$

Show your work.

$\frac{1}{b^4}$

1

$\frac{1}{m^3}$



Examples

Write each fraction as an expression using a negative exponent other than -1 .

e. 8^{-3}

f. 2^{-2}

g. c^{-5}

h. 3^{-3}

$$\frac{1}{3^3}$$

3. $\frac{1}{5^2}$
 $\frac{1}{5^2} = 5^{-2}$

Definition of
negative exponent

4. $\frac{1}{36}$
 $\frac{1}{36} = \frac{1}{6^2}$
 $= 6^{-2}$

Definition
exponent

Definition
negative

Got it? Do these problems to find out.

e. $\frac{1}{8^3}$

g. $\frac{1}{c^5}$

$$\frac{1}{2 \cdot 2 \cdot 2}$$

f. $\frac{1}{4} = \frac{1}{2^2}$

h. $\frac{1}{27}$

$$\frac{1}{3 \cdot 3 \cdot 3}$$

Multiply and Divide with Negative Exponents

The Product of Powers and the Quotient of Powers rules can be used to multiply and divide powers with negative exponents.

Examples

Tutor

Simplify each expression.

6. $5^3 \cdot 5^{-5}$

$$\begin{aligned} 5^3 \cdot 5^{-5} &= 5^{3+(-5)} \\ &= 5^{-2} \\ &= \frac{1}{5^2} \text{ or } \frac{1}{25} \end{aligned}$$

Product of Powers

Simplify.

Write using positive exponents. Simplify.

add

7. $\frac{w^{-1}}{w^{-4}}$

$$\begin{aligned} \frac{w^{-1}}{w^{-4}} &= w^{-1-(-4)} \\ &= w^{(-1)+4} \text{ or } w^3 \end{aligned}$$

Quotient of Powers

Subtract the exponents.

subtract

$$\begin{aligned} 5^2 \cdot 5^3 \\ 5^{2+3} \\ 5^5 \end{aligned}$$

$$\begin{aligned} (5^{-2})^3 \\ = 5^{-6} \end{aligned}$$

multiply!

Show your work.

j. $\frac{1}{729}$

k. $\frac{1}{121}$

$$\begin{aligned} 5^3 \cdot 5^{-5} &= 5^{3+(-5)} \\ &= 5^{-2} \\ &= \frac{1}{5^2} \text{ or } \frac{1}{25} \end{aligned}$$

Product of Powers

Simplify.

Write using positive exponents. Simplify.

7. $\frac{w^{-1}}{w^{-4}}$

$$\begin{aligned} \frac{w^{-1}}{w^{-4}} &= w^{-1-(-4)} \\ &= w^{(-1)+4} \text{ or } w^3 \end{aligned}$$

Quotient of Powers

Subtract the exponents.

Subtract**Got it?** Do these problems to find out.

j. $3^{-8} \cdot 3^2 = 3^{-8+2} = 3^{-6} = \frac{1}{3^6}$

k. $\frac{11^2}{11^4} = 11^{2-4} = 11^{-2} = \frac{1}{11^2}$

l. $n^9 \cdot n^{-4} = n^{9+(-4)} = n^5$

m. $\frac{b^{-4}}{b^{-7}} = b^{(-4)-(-7)} = b^{-4+7} = b^3$

Show your work.

j. $\frac{1}{729}$

k. $\frac{1}{121}$

l. n^5

m. b^3

Lesson 5 Negative

Write each expression using a positive exponent. (Examples 1 and 2)

1. $2^{-4} = \frac{1}{2^4}$

2. $4^{-3} = \frac{1}{4^3}$

3. $a^{-4} = \frac{1}{a^4}$

4. $g^{-7} = \frac{1}{g^7}$

Show your work.

Write each fraction as an expression using a negative exponent other than -1 .

(Examples 3 and 4)

5. $\frac{1}{3^4} = 3^{-4}$

6. $\frac{1}{m^5} = m^{-5}$

7. $\frac{1}{16} = 4^{-2}$ or 2^{-4}

8. $\frac{1}{49} = 7^{-2}$

9. An American green tree frog tadpole is about 0.00001 kilometer in length when it hatches. Write this decimal as a power of 10.

(Example 5) 10^{-5}



length when it hatches. Write this decimal as a power of 10.

(Example 5) 10^{-5}



Simplify. (Examples 6 and 7)

10. $3^{-3} \cdot 3^{-2} = \frac{1}{243}$

11. $r^{-7} \cdot r^3 = \frac{1}{r^4}$

12. $\frac{p^{-2}}{p^{-12}} = p^{10}$

13.  **Building on the Essential Question** How are negative exponents and positive exponents related?

Sample answer: Negative exponents are the result of repeated division and positive exponents are the result of repeated multiplication. You can rewrite an expression with a negative exponent to an expression with a positive exponent by using the multiplicative inverse.

Rate Yourself!

How well do you understand understand negative exponents? Circle the image that applies.



Clear



Somewhat Clear



Not So Clear

Independent Practice

Go online for Step-by-S

Write each expression using a positive exponent. (Examples 1 and 2)

$$1. 7^{-10} = \frac{1}{7^{10}}$$

$$2. (-5)^{-4} = \frac{1}{(-5)^4}$$

$$3. g^{-7} = \frac{1}{g^7}$$

$$4. w^{-13} =$$

Write each fraction as an expression using a negative exponent other than -1 .

(Examples 3 and 4)

$$5. \frac{1}{12^4} = 12^{-4}$$

$$6. \frac{1}{(-5)^7} = (-5)^{-7}$$

$$7. \frac{1}{125} = 5^{-3}$$

$$8. \frac{1}{1,024} =$$

9. The table shows different metric measurements. Write each decimal

Measurem



9. The table shows different metric measurements. Write each decimal as a power of 10. (Example 5) $10^{-1}, 10^{-2}, 10^{-3}, 10^{-6}$

Measurement	Value
Decimeter	0.1
Centimeter	0.01
Millimeter	0.001
Micrometer	0.0001

10. **STEM** An atom is a small unit of matter. A small atom measures about 0.0000000001 meter. Write the decimal as a power of 10.

(Example 5)

$$10^{-10}$$

Simplify. (Examples 6 and 7)

11. $2^{-3} \cdot 2^{-4} = \frac{1}{128}$

12. $s^{-5} \cdot s^{-2} = \frac{1}{s^7}$

13. $y^{-1} \cdot y^4 = y^3$

14. $(3a)(a^{-3}) = \frac{3}{a^2}$

15. $\frac{3^{-1}}{3^{-5}} = 81$

16. $\frac{a^{-4}}{a^{-6}} = a^2$

17. $\frac{y^{-6}}{y^{-10}} = y^4$

18. $\frac{z^{-4}}{z^{-8}} = z^4$

- 19. STEM** The mass of a molecule of penicillin is 10^{-18} kilogram and the mass of a molecule of insulin is 10^{-23} kilogram. How many times greater is the mass of a molecule of penicillin than the mass of a molecule of insulin?

10^5 or 100,000 times

- 20. MP Justify Conclusions** A common flea that is 2^{-4} inch long can jump about 2^3 inches high. About how many times its body size can a flea jump? Explain your reasoning.

2^7 or 128 times; $2^3 \div 2^{-4} = 2^{3 - (-4)}$ or 2^7



H.O.T. Problems Higher Order Thinking

- 21. MP Identify Structure** Without evaluating, order 11^{-3} , 11^2 , and 11^0 from least to greatest. Explain your reasoning.

11^{-3} , 11^0 , 11^2 ; Sample answer: The exponents in order from least to greatest are -3 , 0 , 2 .



22. **MP Identify Structure** Write an expression with a negative exponent that has a value between 0 and $\frac{1}{2}$.

Sample answer: 3^{-2} , $3^{-2} = \frac{1}{3^2}$ or $\frac{1}{9}$

23. **MP Persevere with Problems** Select several fractions between 0 and 1. Find the value of each fraction after it is raised to the -1 power. Explain the relationship between the -1 power and the original fraction.

Sample answer: $\left(\frac{1}{2}\right)^{-1} = 2$, $\left(\frac{34}{43}\right)^{-1} = \frac{43}{34}$, $\left(\frac{56}{65}\right)^{-1} = \left(\frac{65}{56}\right)$; When you

raise a fraction to the -1 power, it is the same as finding the reciprocal of the fraction.

24. **MP Reason Abstractly** For each power, write an equivalent multiplication expression with two factors. The first factor should have a positive exponent and the second factor should have a negative exponent. **Sample answers are given.**

a. $10^4 = 10^6 \cdot 10^{-2}$

b. $8^2 = 8^5 \cdot 8^{-3}$

c. $x^7 = x^{12} \cdot x^{-5}$

