

# 8-3 Study Guide and Intervention

## Multiplying Polynomials

**Multiply Binomials** To multiply two binomials, you can apply the Distributive Property twice. A useful way to keep track of terms in the product is to use the FOIL method as illustrated in Example 2.

**Example 1** Find  $(x + 3)(x - 4)$ .

### Horizontal Method

$$\begin{aligned}(x + 3)(x - 4) &= x(x - 4) + 3(x - 4) \\&= (x)(x) + x(-4) + 3(x) + 3(-4) \\&= x^2 - 4x + 3x - 12 \\&= x^2 - x - 12\end{aligned}$$

### Vertical Method

$$\begin{array}{r} x + 3 \\ \times \quad x - 4 \\ \hline -4x - 12 \\ x^2 + 3x \\ \hline x^2 - x - 12 \end{array}$$

The product is  $x^2 - x - 12$ .

**Example 2** Find  $(x - 2)(x + 5)$  using the FOIL method.

$$\begin{aligned}(x - 2)(x + 5) &\quad \text{First} \quad \text{Outer} \quad \text{Inner} \quad \text{Last} \\&= (x)(x) + (x)(5) + (-2)(x) + (-2)(5) \\&= x^2 + 5x + (-2x) - 10 \\&= x^2 + 3x - 10\end{aligned}$$

The product is  $x^2 + 3x - 10$ .

## Exercises

Find each product.

1.  $(x + 2)(x + 3)$   
 $x^2 + 5x + 6$

2.  $(x - 4)(x + 1)$   
 $x^2 - 3x - 4$

3.  $(x - 6)(x - 2)$   
 $x^2 - 8x + 12$

4.  $(p - 4)(p + 2)$   
 $p^2 - 2p - 8$

5.  $(y + 5)(y + 2)$   
 $y^2 + 7y + 10$

6.  $(2x - 1)(x + 5)$   
 $2x^2 + 9x - 5$

7.  $(3n - 4)(3n - 4)$   
 $9n^2 - 24n + 16$

8.  $(8m - 2)(8m + 2)$   
 $64m^2 - 4$

9.  $(k + 4)(5k - 1)$   
 $5k^2 + 19k - 4$

10.  $(3x + 1)(4x + 3)$   
 $12x^2 + 13x + 3$

11.  $(x - 8)(-3x + 1)$   
 $-3x^2 + 25x - 8$

12.  $(5t + 4)(2t - 6)$   
 $10t^2 - 22t - 24$

13.  $(5m - 3n)(4m - 2n)$   
 $20m^2 - 22mn + 6n^2$

14.  $(a - 3b)(2a - 5b)$   
 $2a^2 - 11ab + 15b^2$

15.  $(8x - 5)(8x + 5)$   
 $64x^2 - 25$

16.  $(2n - 4)(2n + 5)$   
 $4n^2 + 2n - 20$

17.  $(4m - 3)(5m - 5)$   
 $20m^2 - 35m + 15$

18.  $(7g - 4)(7g + 4)$   
 $49g^2 - 16$

**8-3 Study Guide and Intervention** *(continued)***Multiplying Polynomials**

**Multiply Polynomials** The Distributive Property can be used to multiply any two polynomials.

**Example****Find**  $(3x + 2)(2x^2 - 4x + 5)$ .

$$\begin{aligned}
 (3x + 2)(2x^2 - 4x + 5) &= 3x(2x^2 - 4x + 5) + 2(2x^2 - 4x + 5) && \text{Distributive Property} \\
 &= 6x^3 - 12x^2 + 15x + 4x^2 - 8x + 10 && \text{Distributive Property} \\
 &= 6x^3 - 8x^2 + 7x + 10 && \text{Combine like terms.}
 \end{aligned}$$

The product is  $6x^3 - 8x^2 + 7x + 10$ .**Exercises**

Find each product.

1.  $(x + 2)(x^2 - 2x + 1)$

$x^3 - 3x^2 + 2$

2.  $(x + 3)(2x^2 + x - 3)$

$2x^3 + 7x^2 - 9$

3.  $(2x - 1)(x^2 - x + 2)$

$2x^3 - 3x^2 + 5x - 2$

4.  $(p - 3)(p^2 - 4p + 2)$

$p^3 - 7p^2 + 14p - 6$

5.  $(3k + 2)(k^2 + k - 4)$

$3k^3 + 5k^2 - 10k - 8$

6.  $(2t + 1)(10t^2 - 2t - 4)$

$20t^3 + 6t^2 - 10t - 4$

7.  $(3n - 4)(n^2 + 5n - 4)$

$3n^3 + 11n^2 - 32n + 16$

8.  $(8x - 2)(3x^2 + 2x - 1)$

$24x^3 + 10x^2 - 12x + 2$

9.  $(2a + 4)(2a^2 - 8a + 3)$

$4a^3 - 8a^2 - 26a + 12$

10.  $(3x - 4)(2x^2 + 3x + 3)$

$6x^3 + x^2 - 3x - 12$

11.  $(n^2 + 2n - 1)(n^2 + n + 2)$

$n^4 + 3n^3 + 3n^2 + 3n - 2$

12.  $(t^2 + 4t - 1)(2t^2 - t - 3)$

$2t^4 + 7t^3 - 9t^2 - 11t + 3$

13.  $(y^2 - 5y + 3)(2y^2 + 7y - 4)$

$2y^4 - 3y^3 - 33y^2 + 41y - 12$

14.  $(3b^2 - 2b + 1)(2b^2 - 3b - 4)$

$6b^4 - 13b^3 - 4b^2 + 5b - 4$