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## Chapter 4 Practice Test

## SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

## Solve the problem analytically.

1) Of all numbers whose sum is 140 , find the two that have the maximum product. That is, maximize $Q=x y$, where $x+y=140$.
2) Of all numbers whose difference is 18 , find the two that have the minimum product.

## Solve the problem.

3) Find the dimensions that produce the maximum floor area for a one-story house that is rectangular in shape and has a perimeter of 121 ft . Round to the nearest hundredth, if necessary.
4) From a thin piece of cardboard 20 in . by 20 in ., square corners are cut out so that the sides can be folded up to make a box. What dimensions will yield a box of maximum volume? What is the maximum volume? Round to the nearest tenth, if necessary.
5) If the price charged for a bolt is $p$ cents, then $x$ thousand bolts will be sold in a certain hardware store, where $p=42-\frac{x}{18}$. How many bolts must be sold to maximize revenue?
6) Find the number of units that must be produced and sold in order to yield the maximum profit, given the following equations for revenue and cost:
$R(x)=7 x$
$C(x)=0.001 x^{2}+0.9 x+20$.
7) A spherical balloon is inflated with helium at a rate of $110 \pi \mathrm{ft}^{3} / \mathrm{min}$. How fast is the balloon's radius increasing when the radius is 4 ft ?
8) The radius of a right circular cylinder is increasing at the rate of 6 in./s, while the height is decreasing at the rate of $3 \mathrm{in} . / \mathrm{s}$. At what rate is the volume of the cylinder changing when the radius is 5 in . and the height is 11 in .?
9) A man flies a kite at a height of 120 m . The wind carries the kite horizontally away from him at a rate of $8 \mathrm{~m} / \mathrm{sec}$. How fast is the distance between the man and the kite changing when the kite is 130 m away from him?
10) A ladder is slipping down a vertical wall. If the ladder is 20 ft long and the top of it is slipping at the constant rate of $2 \mathrm{ft} / \mathrm{s}$, how fast is the bottom of the ladder moving along the ground when the bottom is 16 ft from the wall?
11) $\qquad$
12) $\qquad$
13) $\qquad$
14) $\qquad$
15) $\qquad$
16) $\qquad$
17) $\qquad$
18) $\qquad$
19) $\qquad$
20) $\qquad$

Testname: CHAPTER 4 CALCULUS PRACTICE TEST

1) 70 and 70
2) 9 and -9
3) $30.25 \mathrm{ft} \times 30.25 \mathrm{ft}$
4) 13.3 in. $\times 13.3$ in. $\times 3.3$ in.; 592.6 in. ${ }^{3}$
5) 378 thousand bolts
6) 3050 units
7) $1.72 \mathrm{ft} / \mathrm{min}$
8) $585 \pi \mathrm{in} .{ }^{3} / \mathrm{s}$
9) $3.1 \mathrm{~m} / \mathrm{sec}$
10) $1.5 \mathrm{ft} / \mathrm{s}$
