

Chapter 6 Practice Test

SCORE _____

Write the letter for the correct answer in the blank at the right of each question.

For Questions 1 and 2, use $f(x) = x + 5$ and $g(x) = 2x^3$.

1. Find $(f \cdot g)(x)$. $2x^3(x+5)$

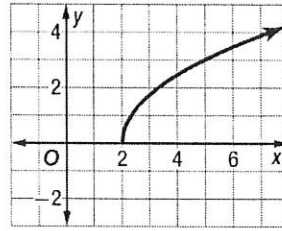
1. $2x^4 + 1$

2. If $f(x) = x^2$ and $g(x) = 3x - 1$ find $[f \circ g](x)$.

$f(g(x))$
 $= (3x - 1)^2$

2. $9x^2 - 6x + 1$

3. State the domain and range of the function graphed.



3. D: $x \geq 2$
 R: $y \geq 0$

4. Find the inverse of $g(x) = -3x + 4$.

$y = -3x + 4$
 $x = -3y + 4$
 $\frac{x-4}{-3}$ OR $\frac{4-x}{3} = y$

4. $f^{-1}(x) = \frac{4-x}{3}$

5. Determine which pair of functions are *not* inverse functions. $f(g(x)) = g(f(x)) = x$

A $g(x) = 2x + 9$ B $g(x) = x - 1$ C $g(x) = 3x - 6$ D $g(x) = 3x + 4$

$h(x) = \frac{1}{2}x - 9$ $h(x) = x + 1$ $h(x) = \frac{1}{3}x + 2$ $h(x) = \frac{x-4}{3}$

5. A

$\frac{1}{2}(2x+9) - 9 = x + 9/2 - 9 \neq x$

6. What is the domain of $y \leq \sqrt{3x + 8}$?

$3x + 8 \geq 0 \rightarrow 3x \geq -8$
 $\frac{3x}{3} \geq \frac{-8}{3}$

6. $x \geq -8/3$

7. Simplify $\sqrt{49x^6y^4}$.

7. $7x^3y^2$

8. Use a calculator to approximate $\sqrt[5]{168}$ to three decimal places.

$\sqrt[5]{168} \approx (168)^{1/5}$

8. ≈ 2.79

9. Simplify $\sqrt[3]{24a^6b^5}$

$\sqrt[3]{(2 \cdot 2 \cdot 2) \cdot (a^2 \cdot a^2 \cdot a^2) \cdot (b \cdot b \cdot b \cdot b \cdot b)}$

$= 2a^2b \sqrt[3]{3b^2}$

9. $2a^2b \sqrt[3]{3b^2}$

10. Simplify $5\sqrt{72} + \sqrt{75} - \sqrt{288}$.

$36 \cdot 2$ $25 \cdot 3$ 144
 $\sqrt{36} \cdot \sqrt{2}$ $\sqrt{5} \cdot \sqrt{3}$ $\sqrt{12} \cdot \sqrt{12}$

$30\sqrt{2} + 5\sqrt{3} - 12\sqrt{2}$

10. $18\sqrt{2} + 5\sqrt{3}$

NAME _____ DATE _____ PERIOD _____

Chapter 6 Practice Test

(continued)

11. Simplify $\frac{3+\sqrt{5}}{3} \cdot (3-\sqrt{5}) = \frac{9-5}{3} = \frac{4}{3}$

12. Write the radical $\sqrt[5]{32m^3}$ using rational exponents. $(32m^3)^{1/5}$

13. Simplify the expression $\frac{x^{5/2}}{x^2}$. $x^{5/2-2} = x^{1/2}$

14. Solve $\sqrt[3]{3m+1} = 4$. $3m+1 = 64 \rightarrow 3m = 63 \rightarrow m = 21$

15. Solve $2 + \sqrt{5x-1} > 5$. $\sqrt{5x-1} > 3 \rightarrow 5x-1 > 9 \rightarrow 5x > 10 \rightarrow x > 2$

16. The velocity of v in feet per second of a roller coaster at the bottom of a hill is related to the vertical drop h in feet and the velocity v_0 in feet per second of the coaster at the top of the hill by the formula $v^2 = v_0^2 + 64h$. What velocity must a coaster have at the top of a 150-foot hill to achieve a velocity of 100 feet per second?

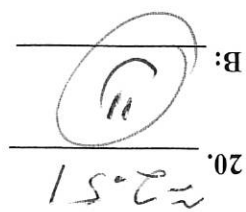
17. TREES The diameter of a tree d (in inches) is related to its basal area BA (in square feet) by the formula $d = \sqrt{\frac{4BA}{\pi}}$. If the basal area of a tree is 12.4 square feet, what is the diameter of the tree? Use a calculator to approximate your answer to three decimal places. Use 3.14 for π .

18. Find the area of a circle whose radius is $3x^5y^3$. Use 3.14 for π . $A = \pi(3x^5y^3)^2 = \pi \cdot 9x^{10}y^6$

19. If x is a positive number, then $\sqrt[5]{x} \div x^{\frac{3}{5}} = ?$

20. The radius r of a sphere with volume V is given by $r = \left(\frac{3V}{4\pi}\right)^{\frac{1}{3}}$. Find the radius of a ball that holds 66 cubic centimeters of air. $r = \left(\frac{3(66)}{4\pi}\right)^{\frac{1}{3}} \approx 2.51$

Bonus If $g(x) = 2x + 1$, find $g[g(x)]$.



Handwritten notes and diagrams for problems 10-16:

- 10. $\frac{9-3\sqrt{5}}{4}$
- 11. $\frac{4}{3}$
- 12. $\frac{1}{5}m, \frac{3}{5}$
- 13. $x^{-1/10}$
- 14. $m = 21$
- 15. $x > 2$
- 16. $v_0 = 20$

Handwritten notes and diagrams for problems 17-20:

- 17. $d = \sqrt{\frac{4(12.4)}{\pi}} \approx 4.769$
- 18. $A = \pi(3x^5y^3)^2 = \pi \cdot 9x^{10}y^6$
- 19. $\sqrt[5]{x} \div x^{\frac{3}{5}} = x^{\frac{1}{5}-\frac{3}{5}} = x^{-\frac{2}{5}} = \frac{1}{x^{\frac{2}{5}}}$
- 20. $r = \left(\frac{3(66)}{4\pi}\right)^{\frac{1}{3}} \approx 2.51$