

Unit 2 Review

(Chapters 3-4)

$$\begin{array}{r} -(x^2 - 4x + 3) \\ - (x-1)(x-3) \\ \hline \end{array}$$

For Questions 1-7, simplify. Assume that no denominator equals 0.

$$\frac{7x^2 + 3x - 9}{(7x^2 + 3x - 9) - (-x^2 + 8x - 3)} =$$

$$2. 5x^3(7x)^2 = 5x^3 \cdot 49x^2 \quad 3. (2x-3)^2$$

$$4. \frac{8y^3 + 27}{2xy - 10y + 3x - 15} = \frac{(2y+3)(4y^2 + 6y + 9)}{(2y+3)(x-5)}$$

$$5y(x-5) + y(x-5)$$

$$6. \sqrt{12} - \sqrt{18} + 3\sqrt{50} + \sqrt{75} = 9\sqrt{3} + 12\sqrt{2}$$

$$\frac{\sqrt{2+i}}{\sqrt{1-3i}} \cdot \frac{\sqrt{1+3i}}{\sqrt{1+3i}} = \frac{\sqrt{2+i} \cdot \sqrt{1+3i}}{1-9i^2} = \frac{-1+7i}{10} = \frac{-1+7i}{10}$$

$$8. \text{ Use synthetic division to find } (2x^3 - 5x^2 + 7x - 1) \div (x-1).$$

$$9. \text{ Write the expression } m^{\frac{7}{9}} \text{ in radical form.}$$

$$10. \text{ Solve } \sqrt{3x+6} + 4 \leq 7. \quad \sqrt{3x+6} \leq 3$$

$$11. \text{ Graph } f(x) = -x^2 + 4x - 3, \text{ labeling the } y\text{-intercept, vertex, and axis of symmetry.}$$

$$\begin{aligned} f(0) &= -3 & x &= \frac{-b}{2a} = \frac{-(-4)}{2(-1)} = \frac{-4}{-2} = 2 \\ y\text{-int} & & & \\ f(+2) &= -(+2)^2 + 4(+2) - 3 & & \\ &= -4 + 8 - 3 = -1 & & \end{aligned}$$

12. The shape of a supporting arch can be modeled by $h(x) = -0.03x^2 + 3x$, where $h(x)$ represents the height of the arch and x represents the horizontal distance from one end of the base of the arch in meters. Find the maximum height of the arch.

$$\text{at Max } x = \frac{-b}{2a} = \frac{-3}{2(-0.03)} = \frac{3}{0.06} = 50$$

13. Solve $2x^2 = 3x + 2$ by graphing. If exact roots cannot be found, state the consecutive integers between which the roots are located.

$$2x^2 - 3x - 2 = 0 \quad (2x+1)(x-2) = 0 \quad x = -\frac{1}{2}, 2$$

14. Solve $x^2 - 2x = 24$ by factoring.

$$x^2 - 2x - 24 = 0$$

15. Write a quadratic equation with $-\frac{3}{4}$ and 4 as its roots. Write the equation in the form $ax^2 + bx + c = 0$, where a , b , and c are integers.

$$4x^2 + 3x - 16x - 12$$

16. Find the exact solutions to $6x^2 + x + 4 = 0$ by using the Quadratic Formula.

$$x = \frac{-1 \pm \sqrt{1-96}}{12} = \frac{-1 \pm \sqrt{-85}}{12} = \frac{-1 \pm i\sqrt{85}}{12}$$

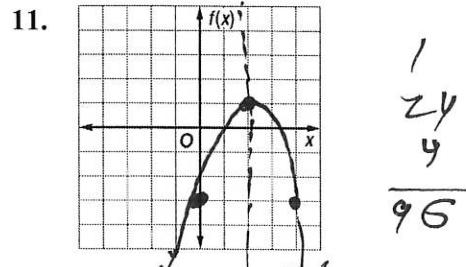
17. Find the value of the discriminant for $9x^2 + 1 = 6x$. Then describe the number and type of roots for the equation.

$$9x^2 - 6x + 1$$

SCORE _____

1. $8x^2 - 5x - 6$
2. $245x^5$
3. ~~$245x^5$~~ $4x^2 - 12x + 9$
4. $\frac{4x^2 + 12x + 9}{x-5}$
5. $4xyz$
6. $9\sqrt{3} + 12\sqrt{2}$
7. $-\frac{1}{10} + \frac{7}{10}i$
8. $2x^2 - 3x + 4 + \frac{3}{x-1}$
9. $\sqrt[9]{m^7}$

$$10. x \leq 1$$



$$\begin{matrix} 1 \\ 2 \\ 4 \\ 9 \\ 6 \end{matrix}$$

$$\begin{matrix} -0.03(2500) + 150 \\ -75 + 150 \end{matrix}$$

$$12. h(50) = 75$$

$$13. x = -2, -\frac{1}{2}$$

$$14. x = -4, 6$$

$$15. 9x^2 - 13x - 12$$

$$16. \text{No real/so/ln/tion}$$

$$17. \text{1 real/so/ln/tion}$$

Unit 2 Review (continued)

18. Identify the vertex, axis of symmetry, and direction of opening for $y = 2(x + 3)^2 - 5$.

19. Write $y = -4x^2 + 8x - 1$ in vertex form.

$$y = -4(x^2 - 2x + 1) - 1 + 4$$

20. Graph $y > x^2 - 2x + 1$.

$$y > (x - 1)^2$$

$0 > 1$ false

For Questions 21 and 22, use the matrices below.

$$A = \begin{vmatrix} 17 & 2 & 3 \\ 11 & 4 & -9 \end{vmatrix} \quad B = \begin{vmatrix} 10 & 6 & -7 \\ -4 & 3 & 0 \end{vmatrix} \quad C = \begin{vmatrix} -1 \\ 2 \\ -2 \end{vmatrix}$$

21. Find $A - B$.

$$\begin{vmatrix} -10 & +12 & -14 \\ 10(-1) + 6(2) + (-7)(-2) \\ (-4)(-1) + (3)(2) + (0)(-2) \\ 4 + 6 + 0 \end{vmatrix} = \begin{vmatrix} -4 \\ 10 \\ 10 \\ 10 \end{vmatrix}$$

22. Find BC , if possible.

$$\begin{vmatrix} x & y \\ 1 & 3 \\ 2 & 4 \end{vmatrix} \text{ Test } (0,0) \text{ false}$$

23. Solve the system of inequalities by graphing.

$$\begin{array}{l} 4x - y \geq 4 \\ 3y < -x + 6 \end{array}$$

$$\begin{array}{|c|c|} \hline x & y \\ \hline 0 & 2 \\ 3 & 1 \\ \hline \end{array} \text{ Test } (0,0) \text{ true}$$

24. Evaluate $\begin{vmatrix} 12 & 5 & -2 & 12 \\ -3 & 0 & 1 & 1 \\ -5 & 4 & 2 & 5 \\ 0 & 4 & 0 & 0 \end{vmatrix}$ using diagonals.

25. Use Cramer's Rule to set up the solution for y of equations $3x - 5y = 21$ and $4x + 2y = 2$. Do not solve.

26. Solve the matrix equation $\begin{vmatrix} 4 & -5 \\ 1 & 2 \end{vmatrix} \cdot \begin{vmatrix} m \\ n \end{vmatrix} = \begin{vmatrix} 32 \\ -5 \end{vmatrix}$ using the inverse matrices. OR...

$$\begin{aligned} 2(4m - 5n) &= 32 \\ 5m + 2n &= -5 \end{aligned} \text{ then solve...}$$

$$\begin{aligned} 8m - 10n &= 64 \\ 5m + 10n &= -25 \end{aligned}$$

$$\begin{aligned} 13m &= 39 \\ m &= 3 \end{aligned}$$

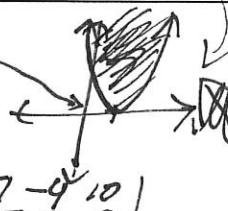
$$\begin{aligned} 9(3) - 5n &= 32 \\ 12 - 5n &= 32 \end{aligned}$$

$$\begin{aligned} -5n &= 20 \\ n &= -4 \end{aligned}$$

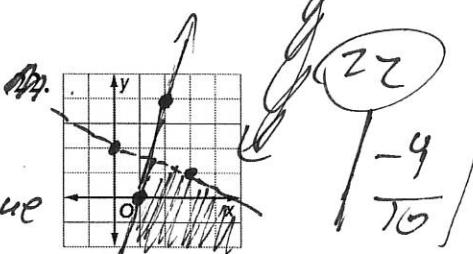
18. opens up $\left\{ \begin{array}{l} ax^2 + bx + c \\ x = -3 \end{array} \right\} (-3, -5)$

19. $y = -4(x - 1)^2 + 3$

20. _____



21. $\begin{vmatrix} 7 & -4 & 10 \\ 15 & 0 & -9 \end{vmatrix}$



23. π

24. _____

25. y

26. $(3, -4)$

25. $y = \begin{vmatrix} 3 & 2 \\ 4 & 2 \end{vmatrix}$

$$\begin{vmatrix} 3 & -5 \\ 4 & 2 \end{vmatrix}$$