

Find the exact length of the curve analytically by antidifferentiation.

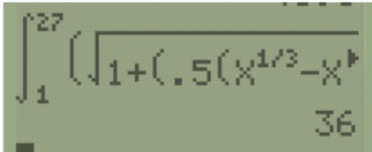
1)  $y = \frac{3}{8}(x^{4/3} - 2x^{2/3})$  from  $x = 1$  to  $x = 27$

1) \_\_\_\_\_

A) 93                      B)  $\frac{87}{2}$   
 C)  $\frac{153}{4}$                       D) 36

①  $\frac{dy}{dx} = \frac{3}{8} \left( \frac{4}{3} x^{1/3} - \frac{4}{3} x^{-1/3} \right) dx$   
 $= \frac{1}{2} (x^{1/3} - x^{-1/3})$

$L = \int_1^{27} \sqrt{1 + \left( \frac{1}{2} (x^{1/3} - x^{-1/3}) \right)^2} dx$



3)  $x = \frac{y^4}{8} + \frac{1}{4y^2}$  from  $y = 1$  to  $y = 2$   $\frac{1}{4} y^{-2}$

3) \_\_\_\_\_

A)  $\frac{33}{8}$

B) 2

C)  $\frac{33}{16}$

D)  $\frac{17}{8}$

$$L = \int_1^2 \sqrt{1 + \left(\frac{dx}{dy}\right)^2} dy$$

$$\frac{dx}{dy} = \frac{1}{2} y^3 - \frac{1}{2} y^{-3}$$

$$L = \int_1^2 \sqrt{1 + \left(\frac{1}{2} y^3 - \frac{1}{2} y^{-3}\right)^2} dy$$

33/16	2.0625
$\int_1^2 \sqrt{1 + (.5x^3 - .5x^{-3})^2}$	2.0625